

House loans decisive factors (or features) comparison: helping customers get loans

Lingxiao He¹,

Zhekai Yu^{2*},

Chenshirui Wang³,

Yue'er Yang⁴

¹International Department, Qingdao No.58 Middle School, Qingdao, 266000, China, Douglass.hlx@outlook.com

²Edmonds college, Lynnwood, 98026, the United States, 15337243239y@gmail.com

³Merchiston International School, Shenzhen, 518000, China, rruimw704@outlook.com

⁴Zhejiang Province Hangzhou No.2 Middle School, Hangzhou, 310053, China, 18868871096@163.com

*Corresponding author email: 15337243239y@gmail.com

Abstract:

This article provides a method, system, and related equipment for comparing decisive factors of house loans to assist consumers in securing loans. We chose the data that includes many factors about personal such as marriage/single, income. The study was conducted applying decision tree, neural network, and logic regression. The method includes obtaining consumer financial data; segmenting this data into multiple overlapping financial facets; generating a preliminary financial profile from these facets; performing noise reduction on the preliminary profile to create a detailed financial model; slicing the detailed model into various financial segments; and analyzing these segments to derive a multidimensional understanding of key house loan factors. This approach minimizes both explicit and implicit risks, ensuring a precise alignment with consumer financial profiles. Additionally, converting three-dimensional financial data into two-dimensional segments reduces computational complexity and errors, ensuring overall accuracy in loan evaluation and decision-making. In the last, we use these models to compare which factor influence the risk of loan mostly, so we advise if customers do not have house or car, keep working in one field and carefully view different places' loan policies still can be helpful for their loaning.

Keywords: decision tree, neural network, logic regression, prediction, house loans, mortgage loans, consumers.

1. Introduction

Nowadays unstable economic environment requires banks to be more rigorous in their approach to lending, and the factors affecting lending have become more varied. But we discover that there is too much research talk about which model can best predict the loan default or availability. So we want to try

the different way that focuses on which factors will significantly affect the loaning availability. The main features we cover include credit score, income stability, down payment, debt-to-income ratio, profession, professional experience, city, married or single, house ownership and car ownership. And the models we use in this paper are Decision Tree, Neural Network, Logistics Regression.

A high credit score often results in lower interest rates and better loan terms. Consistent income and employment history reassure lenders of repayment capability. A substantial down payment can reduce loan amount and monthly payments, while a favorable debt-to-income ratio indicates manageable debt levels relative to income. Professional experience, on the other hand, shows how stable a person's life is in general. A stable marriage refers to greater ability to pay, in addition, with kids and parents to support, applicant will have to spend more money on basic life. Ownership of cars and houses make sure the banks can get the money back because they can serve as a pledge if applicant fails to pay the debt. Different cities represent different rates of consumption.

2. Literature Review

The prediction of house loan approval is a critical topic in finance, aiming to improve loan granting efficiency and minimize defaults. This literature review explores key studies on predicting loan defaults using decision trees, neural networks, and logistic regression, providing insights into their methodologies, findings, and contributions.

Li et al. (2022) proposes a multi-model fusion approach for loan default prediction, highlighting the effectiveness of integrating various models to enhance accuracy. Their study underscores the importance of combining different techniques for robust predictions.^[9]

Wang et al. (2023) apply a heterogeneous ensemble learning approach and SHAP method to predict national student loan defaults. This research emphasizes the significance of interpretability in machine learning models, demonstrating how SHAP values can provide insights into feature importance.

Li and Wu (2024) focus on explainable machine learning for loan default predictability. Their findings stress the necessity of transparency in predictive models, which can build trust and provide clear justifications for loan approval decisions.^[10]

Ayberk and Önder (2022) explore the relationship between house prices and bank loan portfolios, particularly the role of bank ownership. Their study reveals how external economic factors, and institutional characteristics influence loan decisions.^[11]

The reviewed literature highlights the evolving landscape of loan default prediction, with multi-model approaches and interpretability being central themes. While these studies contribute significantly to the field, further research is needed to refine predictive models and explore additional factors influencing loan approval.

3. Models and Methods

Logistic Regression:

Logistic regression is a statistical method for binary classification tasks. It models the probability that a given input belongs to a particular class. As for binary variables, they can be generalized to categorical variables when there are more than two possible values.^[1]

Formula:

m is the midpoint of the logistic curve (the location parameter), and s is scale parameter which makes the distribution more spread out as it gets larger.

In this variable formula, (we've known the $y = b_0 + b_1x$)^[2]

$b_0 = -m/s$, is the y-intercept.

$b_1 = 1/s$, is the rate parameter.

A common way to measure the goodness of fit of logistic regression is to use logical loss (also known as log loss), or negative log-likelihood.

For given x_k and y_k in the regression:

We use p_k to represent the probabilities of y_k equals to 1 (which means the house loans could be permitted in this research);

On the contrary, the $1-p_k$ are the probabilities that they will be zero (which means the house loans are not permitted in this research)

Usually, we use ℓ_k to present the log loss of the data and define it:^[1]

$$y_k = 1, \ell_k = -\ln p_k$$

$$y_k = 0, \ell_k = -(1 - \ln p_k)$$

Since Log loss is always greater than or equal to 0, equals 0 only in case of a perfect prediction, and approaching infinity as the prediction gets worse. And in a logistic regression it is not possible to have zero loss at any points, since y_k is either 0 or 1, but $0 < p_k < 1$.

Combining with log loss formulas above because they are measuring a same event's different results, we can get new formula:

In professional words, this expression is more formally known as the cross-entropy of the predicted distribution ($p_k, (1-p_k)$) from the actual distribution ($y_k, (1-y_k)$),

On the contrary, we could use the Log Loss formula to maximize the Log-likelihood:^[1]

$$\iota = \sum_{k: y_k=1} \sum_{k: y_k=0} \ln(1-p_k) = \sum_{k=1}^K (y_k \ln(p_k) + (1-y_k) \ln(1-p_k))$$

Decision Tree Learning

Decision tree learning is a supervised learning approach. In this learning, we use classification and regression Decision Tree as a model to predict our dataset.

A tree model in which the target variable can take a set of discrete values is called a classification tree. In these tree-like structures, leaves represent class labels, and branch-

ing tables represent the conjunctions of features that lead to these class labels.

There are many different kinds of Decision Tree: ^[4]

ID3 (Iterative Dichotomiser 3)

C4.5 (successor of ID3)

CART (Classification and Regression Tree)

OC1 (Oblique classifier 1). First method that created multivariate splits at each node.

Chi-square automatic interaction detection (CHAID). Performs multi-level splits when computing classification trees.

In our research, we mainly use CART to analyze the house loans because it is the most efficient and general one.

Decision Tree method is used mainly in two main types:

1. Classification Tree: Predict the result category of the desired data, such as defining faces to human class and cat faces to animal class.

2. Regression Tree: Regression tree analysis is used when we want to get a real number when predicting, such as the price of house loan or the years people have spent on recent jobs.

Advantages: intelligibility and simplicity.

Dataset form: $(x, Y) = (x_1, x_2, x_3, \dots, x_k, Y)$ ^[4]

Metrics

Since the decision tree is constructed from the top down, the best variable is selected (split) through each branch of the tree, and different Metrics are developed to measure whether this action is the “best”.

Gini impurity

In our experiments, we mainly use Gini impurity to measure the “best” since Gini impurity was first developed by analyzing with CART algorithms for classification trees. With similar situations of Corrado Gini, thus we choose Gini impurity.

Gini Impurity value is between 0 and 0.5,

The closer to 0, the better splits done by CART is.

The closer to 0.5, the worse splits done by CART is.

For a set of items with J classes and relative frequencies $p_i, i \in \{1, 2, 3, \dots, J\}$, the probability of choosing an item with label i is p_i , and the probability of mis categorizing that item is $\sum_{(k \neq i)} p_k = 1 - p_i$.

Then, we can sum up all the pairwise products of these probabilities for each label. ^[5]

Neural Network

An artificial neural network consists of connecting units, or nodes, of artificial neurons that loosely mimic neurons in the brain.

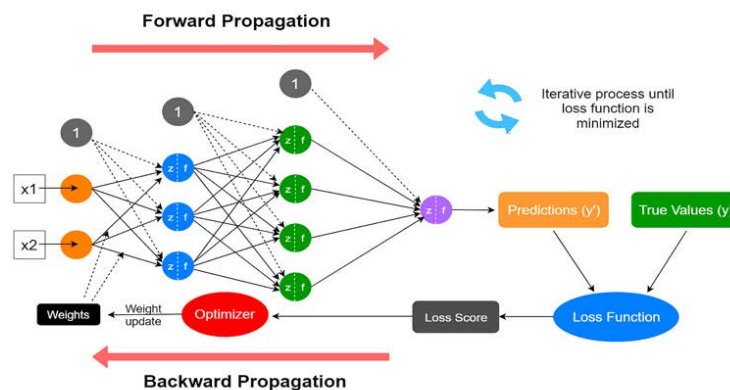
They are connected by the edge, which mimics the synapses in the brain and the way nerves transmit electrical signals. Each artificial neuron receives signals from connected neurons, then processes those signals and sends the signals to other connected neurons.

In machine learning, the “signal” is a real number, and the output of each neuron is calculated as a nonlinear function of the sum of its inputs, called the activation function.

The signal strength at each connection is determined by a weight, and the optimal solution is found by repeating the balance weight several times.

Advantages:

1. Neural networks that can work continuously and are more efficient than humans or simpler analytical models. [6]
2. Using algorithmic computing in the cloud can reduce risks such as data breaches.
3. This is the Most comprehensive and complicated model, which fits mostly to all situations when put into varies industries to analyze and predict.
4. It can be programmed to learn from prior outcomes to strive to make smarter future calculations. [6]



Convolutional Neural Networks and Deconvolutional Neural Networks

The data of a convolutional neural network is divided into multiple layers, including an input layer, an output layer, and a large number of hidden convolutional layers in the middle for "thinking". The whole process is like our linear thinking, the cause goes through the effect, and finally comes to the desired conclusion.

Formula: $Y = \beta_0 + \beta_1 \cdot x_1 + \beta_2 \cdot x_2 + \beta_3 \cdot x_3 + \dots + \beta_k \cdot x_k + \epsilon$

Deconvolution neural network is the category that we use most in the analysis of weights, which is the reverse of the convolutional neural network. After many more neural networks "thinks", we can reverse the search for the weights of each independent variable x . It's like reverse thinking in humans. In this research, it can help us to advise borrowers and make it easier for them to get loans.

4. Experiment and research

4.1 Data processing

In this paper, the database we use is Loan Prediction Based on Customer Behavior, which is open source on Kaggle website. And the whole original dataset has 252,000 loan data from all different individuals, with 13 columns.

Data Balance:

Features (factors)	Description	Data Type
Income	Income of the user	Int
Age	Age of the user	Int
Experience	Professional experience of the user in years	Int
Married/ Single	Whether married or single	String
House_Ownship	Owned or rented or neither	String
Car_Ownship	Does the person own a car	String
States	The state people live in	String
Current_House_Yrs	Years of experience in the current residence	Int
Risk_Flag	Defaulted on a loan	String

Y: "0" = refuse/ deny the house loans; "1" = accept the applications of house loans.

After analyzing by the Neural Network, it found out the most credible ranking of the importance of the effective factors.

First, there are too many "0" in the Dependent variable, which means most of the applications for house loans were denied by the banks in the original chosen dataset. Thus, we need to balance the data probabilities in our chosen dataset by using the method of sampling balance. To be specific, in this research, we increase the weight of "1" (means access the house loans) in the dataset to make sense for the predictions.

Data cleaning:

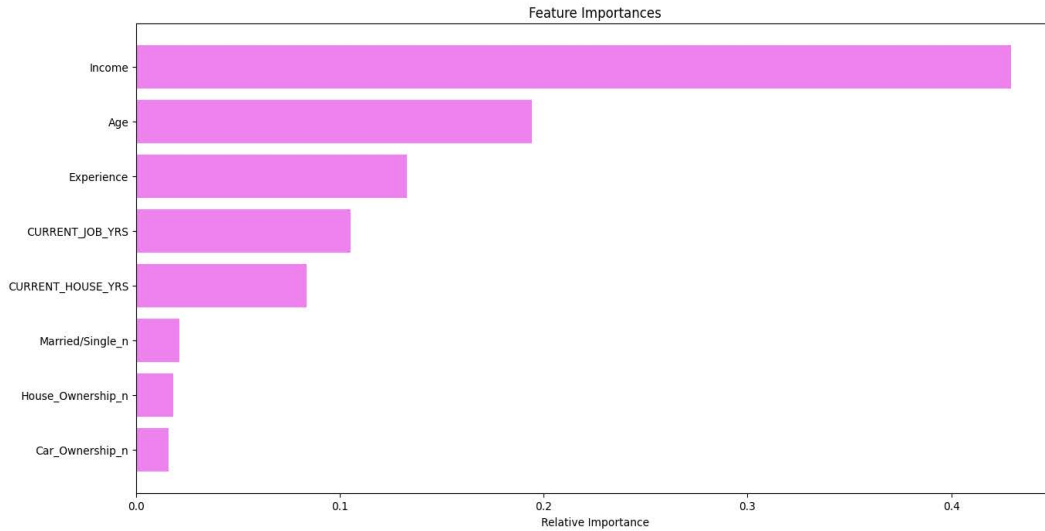
The team has checked all the columns in the original dataset. Some columns are pretty homogeneous, such as the city and the state, which might influence the accuracy of the analyzing, thus we delete the column.

The whole training data 252,000 individuals which is too much to make analysis and prediction without any overfitting. Thus, we used python to randomly choose 20,000 unique (approximately 8.7%) values in the training data by programming.

4.2 Independent Variables

After the data cleaning, we deleted City, ID, Profession since they are not really related to the Risk_Flag many. This is caused by the uniqueness of these factors, causing the weight to become too low.

We Keeps income, age, Experience, house/car owning and some other high correlation factors.



As shown above, neural network has automatically learned the sample dataset. **4.3 EDA**

```

1 "E:\Users\15337\PycharmProjects\Hello python\pythonProject1\.venv\Scripts\python.exe" "E:\Users\15337\PycharmProjects\Hello
python\pythonProject1\orange3"
2 <class 'pandas.core.frame.DataFrame'>
3 RangeIndex: 252000 entries, 0 to 251999
4 Data columns (total 9 columns):
5 # Column Non-Null Count Dtype
6 ---
7 0 Income 252000 non-null int64
8 1 Age 252000 non-null int64
9 2 Experience 252000 non-null int64
10 3 CURRENT_HOUSE_YRS 252000 non-null int64
11 4 Married/Single_n 252000 non-null int32
12 5 House_Ownership_n 252000 non-null int64
13 6 Car_Ownership_n 252000 non-null int32
14 7 Profession_n 252000 non-null int64
15 8 State_n 252000 non-null int64
16 dtypes: int32(2), int64(7)
17 memory usage: 15.4 MB
18 None
19
20 Process finished with exit code 0
21
    
```

```

1 "E:\Users\15337\PycharmProjects\Hello python\pythonProject1\.venv\Scripts\python.exe" "E:\Users\15337\PycharmProjects\Hello
python\pythonProject1\orange3"
2
3 count 2.520000e+05 252000.000000 ... 252000.000000 252000.000000
4 mean 4.997117e+06 49.954071 ... 0.023639 0.202873
5 std 2.878311e+06 17.063855 ... 0.151922 0.603813
6 min 1.031000e+04 21.000000 ... 0.000000 0.000000
7 25% 2.503015e+06 35.000000 ... 0.000000 0.000000
8 50% 5.000694e+06 50.000000 ... 0.000000 0.000000
9 75% 7.477502e+06 65.000000 ... 0.000000 0.000000
10 max 9.999938e+06 79.000000 ... 1.000000 2.000000
11
12 [8 rows x 9 columns]
13
14 Process finished with exit code 0
15
    
```

Before we build the models, we need to preprocess the data. This part will skip introducing the common preprocessing data but put more concentration on our special works for data.

First, our data is not balanced data, for example, in our features “House_Ownership” that column, “rented” take 92% place, this will cause our models especially for classification models to ignore the effect of “owned” feature since “owned” just has 3%. This problem also occurred

in dependent variable “Risk_Flag”. In “Risk_Flag”, 0 is the majority, so it will let the model believe that some features changing will not make sense. Thus, we balanced the training data after we splitted the test and train data to build the models.

Second, we dropped two columns “CITY” and “CURRENT_JOB_YRS”. The reason we made this decision was because both columns overlapped. In the data frame, we have “STATE” and “CITY” two features, but they are

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too similar, they all represent the feature of area, if we want to see what will bring to dependent variable by the feature of area, we want to see only one column to represent the feature of area since it is clear and easier to build the models. And "CITY" is more complex than "STATE", so we chose "STATE" as our feature of area. Also, "Experience" and "CURRENT_JOB_YRS" are similar, too. "Experience" is the feature that measures the customer's professional experience in years like how many years you work in this field. "CURRENT_JOB_YRS" is how many years does customer works in this job. The short of "CURRENT_JOB_YRS" is when the customer changes the job, this feature will come to 0. Thus, if we try to know how

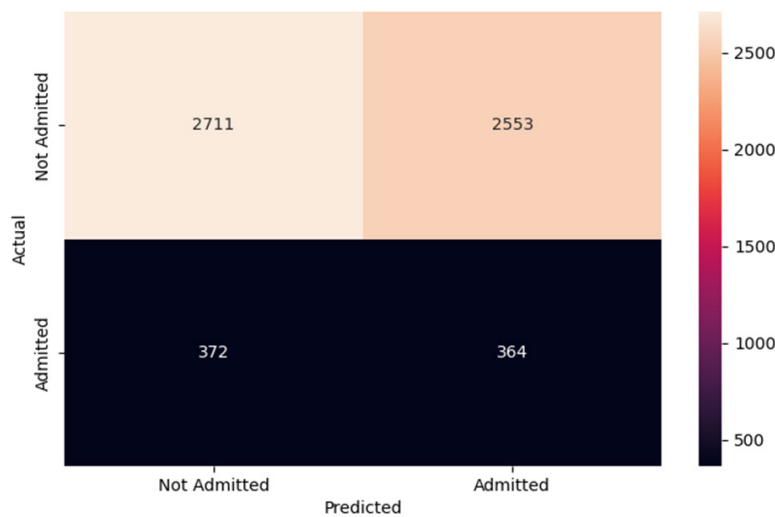
many years a customer stays in one field, "Experience" is better than "CURRENT_JOB_YRS".

Third, we scaled the data. "Income" is the special one column since the number of this feature is too big, we want to decrease the influence of big numbers. Thus, we scaled the data.

4.4 Data Analysis and Prediction by models

Following the standard procedure of verifying the accuracy and conformity of the model, the three models were all programmed to produce the accuracy and other measuring standards after the analyzing and prediction.

4.4.1 Logistic Regression



```

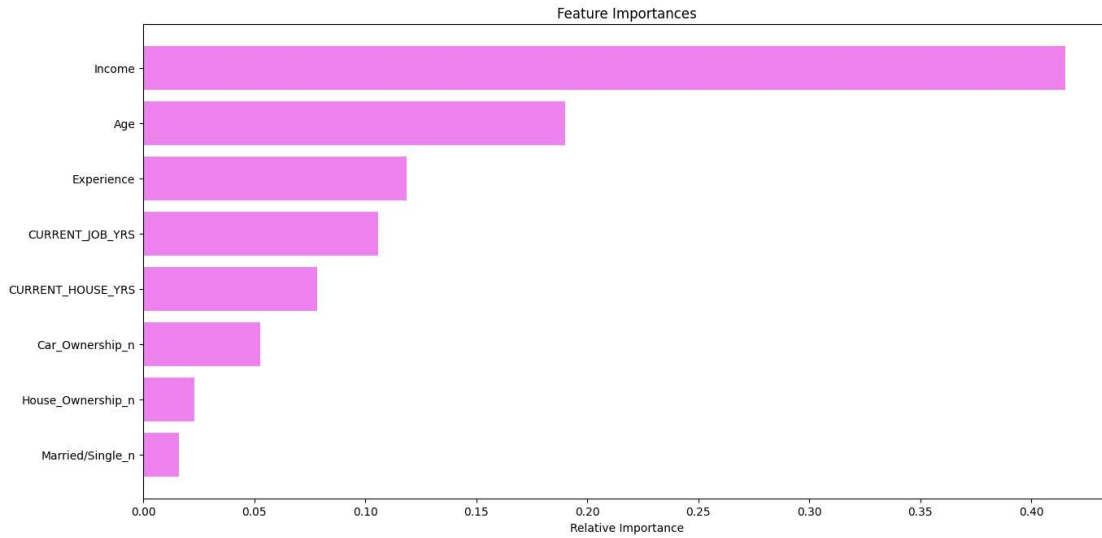
1 "E:\Users\15337\PycharmProjects\Hello python\pythonProject1\.venv\Scripts\python.exe" "E:\Users\15337\PycharmProjects\Hello python\pythonProject1\apple 2"
2 0.5301666666666667
3 [[2803 2482]
4 [ 337 378]]
5 Recall on training set: 1.0
6 Recall on test set: 0.5286713286713287
7 Normalized Confusion Matrix:
8 [[0.53036897 0.46963103]
9 [0.47132867 0.52867133]]
10 E:\Users\15337\PycharmProjects\Hello python\pythonProject1\.venv\Lib\site-packages\sklearn\base.py:486: UserWarning: X has feature names, but LogisticRegression was
11 warnings.warn(
12 precision recall f1-score support
13
14 0 0.89 0.53 0.67 5285
15 1 0.13 0.53 0.21 715
16
17 accuracy 0.53 6000
18 macro avg 0.51 0.53 0.44 6000
19 weighted avg 0.80 0.53 0.61 6000
20
21 Optimization terminated successfully.
22 Current function value: 0.647318
23 Iterations 6
24
25 =====
26 Dep. Variable: Risk_Flag No. Observations: 24486
27 Model: Logit Df Residuals: 24477
28 Method: MLE Df Model: 8
29 Date: Fri, 02 Aug 2024 Pseudo R-squ.: 0.06612
30 Time: 06:38:48 Log-Likelihood: -15850.
31 converged: True LL-Null: -16972.
32 Covariance Type: nonrobust LLR p-value: 0.000
33 =====
34 coef std err z P>|z| [0.025 0.975]
35 -----
36 Income 2.922e-08 4.55e-09 6.417 0.000 2.03e-08 3.81e-08
37 Age 0.0021 0.001 2.711 0.007 0.001 0.004
38 Experience -0.0252 0.002 -10.663 0.000 -0.030 -0.021
39 CURRENT_HOUSE_YRS 0.0249 0.005 5.090 0.000 0.015 0.035
40 Married/Single_n 0.0142 0.040 0.356 0.722 -0.064 0.092
41 House_Ownership_n -1.6908 0.102 -16.502 0.000 -1.892 -1.490
42 Car_Ownership_n -0.9880 0.034 -29.288 0.000 -1.054 -0.922
43 Profession_n -0.2313 0.052 -4.440 0.000 -0.333 -0.129
44 State_n -1.6619 0.071 -23.413 0.000 -1.801 -1.523
45 =====
46
47 Process finished with exit code 0

```

As the graph shown above, after balancing the "1" individuals and "0" individuals in the sampling dataset, we

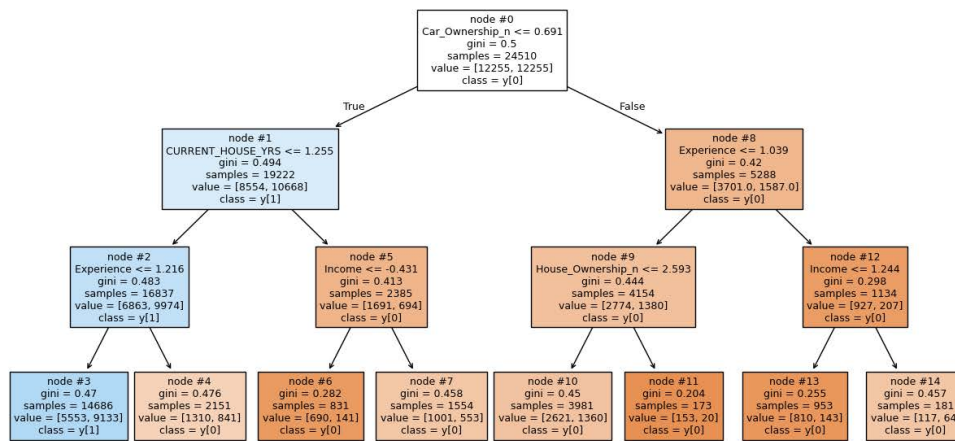
have deleted some of the atypia. Thus, it is obvious the total unique values in the statistic graph above is less than 20,000. Now there are 6,000 individuals available, the approximate accuracy of prediction is better than before.

Although it does not seem a really good number, the accuracy is still good to use in most situations since the real data could not be perfect.

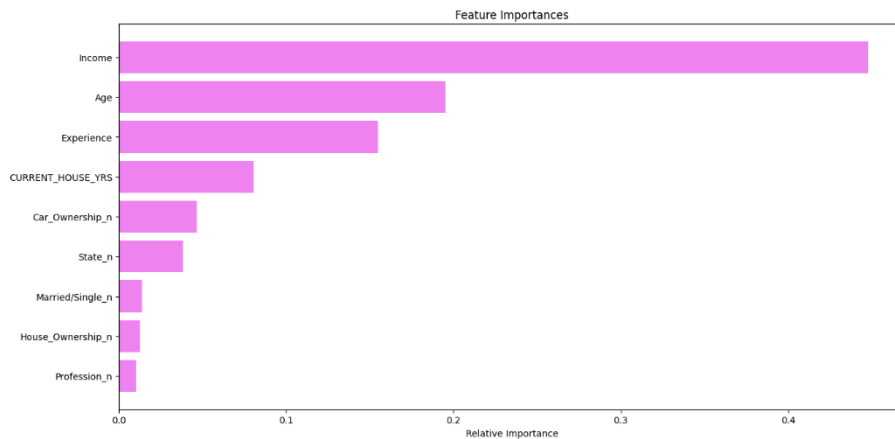


4.4.2 Decision Tree

Hyperparameter: Max_Depth = 4.
The tree after split:

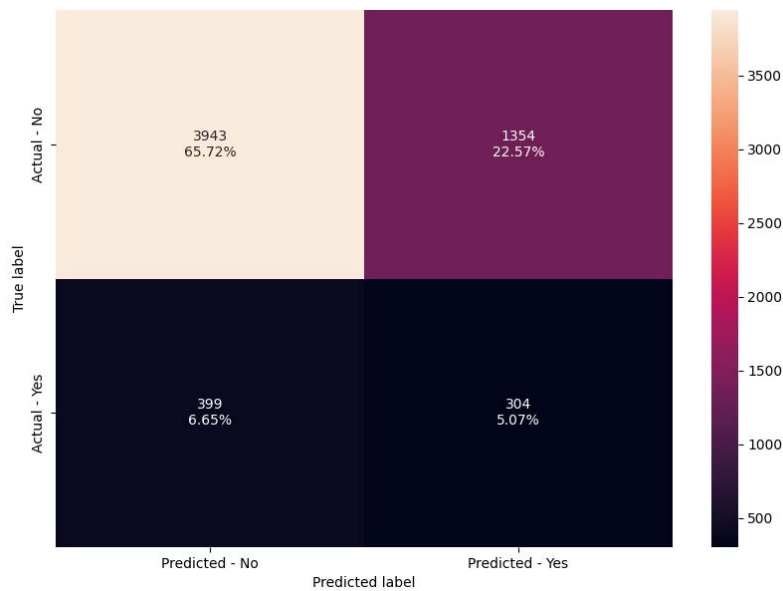


The decision tree model is shown in the first graph. The class in the last row in each leaf could easily show the result of the application. And in the third row in each leaf, we can get the Gini Impurity calculated by Decision Tree model built by python.



Accuracy calculated by Python:
 Accuracy of test: 0.7078333333333333
 Accuracy of train: 0.9792329661362709

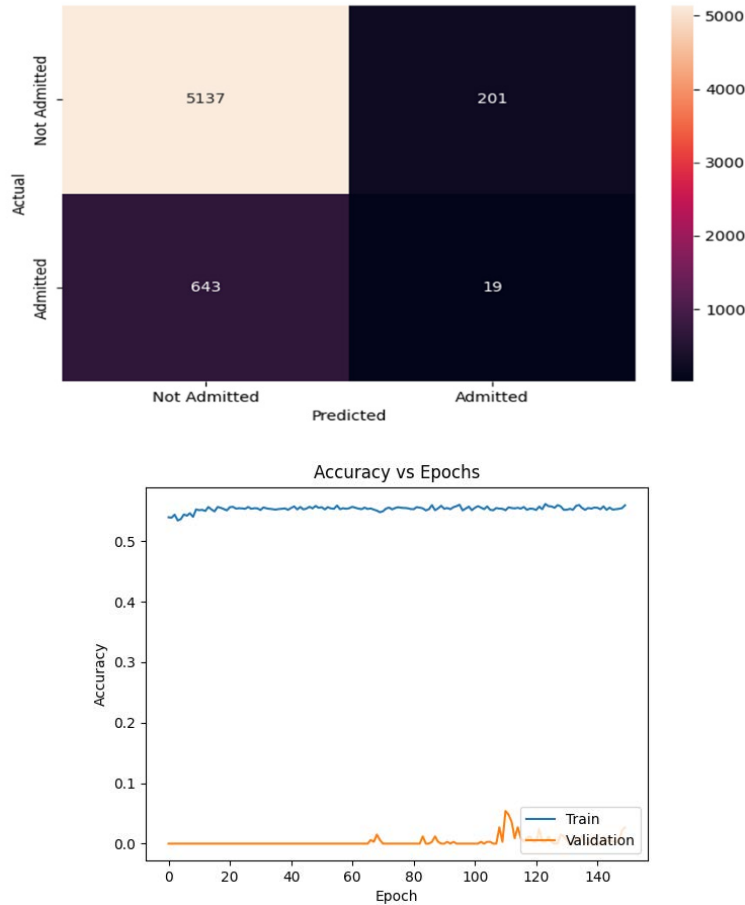
Recall on training set: 0.9773969808241534
 Recall on test set: 0.43243243243243246



In the second graph, the total rate for predicting correctly is $65.72\% + 5.07\% = 70.79\%$, which is such a fantastic accuracy for Analysis and Prediction in Decision Tree model, using the real, normal data. The result shown above indicates the model predicts the people (both pre-

dicted and actual are NO), however, the people (both predicted and actual are yes) were predicted far less well. Finally, the decision tree gives the best matching analyzing.

4.4.3 Neural Network



The accuracy of the Neural network in training is approximately 0.55 and the validation (Testing) is approximately. Even though the model fits the training data not bad, when it fits the testing data, the accuracy almost is 0. So, this model does not learn well.

Data Analyzing enhance

After analyzing the dataset, all the three chosen models indicate the income is the most effective variable among all. Then, it is necessary to check the conclusion before it comes to a theory that could be shown to the consumers. As usual, P-value is used to measure the significant level of income to make sure it is totally independent. However, after calculation, the significant level is too low (we can find through P-value), much lower than the $\alpha = 0.05$ and 0.01 . Thus,

the income is a proper independent variable which could be used in analysis and prediction.

To find the real determinable factors, logistic regression was used to calculate all

P-value of the relevant factors in the sampling dataset.

In the table, it is shown that the absolute value of P-value of the Car_Ownership is

0 and House_Ownership is 0, so we can make sure that Car_Ownership and House_Ownership are the features

can really influence the result, but the P-value of Marriage/Single is too high to say it is not enough to affect the result. Then, we can see the coefficients of those factors to determine which one has the most influential to the result.

For example, the coefficients of the House_Ownership has the most distance from 0, so we can say that House_Ownership has the largest impact on the result.

Logit Regression Results

Dep. Variable	y	No. Observations	8787
Model	Logit	Df Residuals	8776
Method	MLE	Df Model	10
Date	Wed, 31 Jul 2024	Pseudo R-squ	0.04260

Time	16:59:00	Log-Likelihood	-5830.8
Converged	True	LL-Null	-6090.2
Covariance Type	no robust	LLR p-value	4.129e-105

	coef	Std err	z	P> z	[0.025	0.975]
Income	2.922e-08	4.55e-09	6.417	0.000	2.03e-08	3.81e-08
Age	0.0021	0.001	2.711	0.007	0.001	0.004
Experience	-0.0252	0.002	-10.663	0.000	-0.030	-0.021
CURRENT_HOUSE_YRS	0.0249	0.005	5.090	0.000	0.015	0.035
Marriage/Single_n	0.0142	0.040	0.356	0.722	-0.064	0.092
House_Ownership_n	-1.6908	0.102	-16.502	0.000	-1.892	-1.490
Car_Ownership_n	-0.9880	0.034	-29.288	0.000	-1.054	-0.922
Profession_n	-0.2313	0.052	-4.440	0.000	-0.333	-0.129
State_n	-1.6619	0.071	-23.413	0.000	-1.801	-1.523

5. Conclusion

This article explores decisive factors for house loans and compares methods to assist customers in securing loans. The study employs decision trees, neural networks, and logistic regression. The methodology involves acquiring consumer financial data, segmenting it to create a preliminary financial profile, reducing noise, and analyzing the data to identify key loan factors. Key features analyzed include income, age, professional experience, marital status, and house/car ownership. Results indicate that decision tree models have the highest accuracy (70.79%) respectively. The study highlights the importance of these factors in loan approval and provides a precise, multi-dimensional understanding of loan decision-making, ultimately aiding consumers in obtaining loans more effectively. Finally, the State_n and House_Ownership is determined to be the most effective factors (independent variables) for this mortgage loans analysis for consumers because they have the highest coefficients which means they are most relevant largely influential variables in the research. Combined with financial analyzing by, the banks are more willing to lend the house loans to people who have houses, but different area may have different policy about loaning^[7]. Therefore, the result suggests if customers have car and house, bank is willing to lend you money. But if you do not have those things, put more concentration on the policy of different area about your loan and staying in one job or field more years to get more experience.

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sidered co-first authors.

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